

## NON-STANDARD MATRIX PROBLEMS

**Norieva Aziza Jasur qizi**

Jizzakh branch of National University of Uzbekistan  
named after Mirzo Ulugbek, assistant.

[noriyevaaziza@gmail.com](mailto:noriyevaaziza@gmail.com)

### **ABSTRACT**

*In this article, one of the main sections of the science of algebra and number theory, non-standard problems related to matrices were seen. From the article, students can study higher mathematics, algebra and number theory independently or under the guidance of a professor. It can be used by students, young people and those interested in mathematics.*

**Keywords:** matrix, non-standard problem, rank, degree, elementary divisor.

### **INTRODUCTION**

Matrices are one of the main branches of algebra and number theory, and the dictionary meaning of the word matrix is a table made up of rectangular numbers. When solving systems of equations and any related problems, we encounter matrices. It is known that the numbers that make up the matrix are called its elements. [1]

### **METHODS**

The following operations are appropriate on matrices: addition, subtraction, multiplication by a number. There is no concept of dividing a matrix by a matrix. Instead, the first matrix is multiplied by the second matrix. Such matrices can be added and subtracted only if the orders of the matrices are the same, that is, if the number of columns and rows of the matrices are equal, respectively. Only the inverse of a square matrix exists. [1]

## RESULT

*Matter.*  $A = \begin{pmatrix} \lambda^2 - \lambda + 4 & \lambda^2 + 3 \\ \lambda^2 - 2\lambda + 3 & \lambda^2 - \lambda + 2 \end{pmatrix}$  matrix color is equal to 2 at what value of  $\lambda$ .

*Solving.*

$$\begin{aligned} A &= \begin{pmatrix} \lambda^2 - \lambda + 4 & \lambda^2 + 3 \\ \lambda^2 - 2\lambda + 3 & \lambda^2 - \lambda + 2 \end{pmatrix} \sim \begin{pmatrix} \lambda + 1 & \lambda + 1 \\ \lambda^2 - 2\lambda + 3 & \lambda^2 - \lambda + 2 \end{pmatrix} \sim \\ &\sim \begin{pmatrix} \lambda + 1 & 0 \\ \lambda^2 - 2\lambda + 3 & \lambda + 1 \end{pmatrix} \sim \begin{pmatrix} \lambda + 1 & 0 \\ \lambda^2 - 2\lambda + 3 & \lambda + 1 \end{pmatrix} \sim \begin{pmatrix} \lambda + 1 & 0 \\ 6 & \lambda + 1 \end{pmatrix} \end{aligned}$$

So,  $\lambda + 1 \neq 0$ ,  $\lambda \neq -1$ .

*Matter.* Find the elementary divisors of the following matrix:

$$\begin{pmatrix} \lambda^3 + 2 & \lambda^3 + 1 \\ 2\lambda^3 - \lambda^2 - \lambda + 3 & 2\lambda^3 - \lambda^2 - \lambda + 2 \end{pmatrix}$$

*Solving.*

$$\begin{pmatrix} \lambda^3 + 2 & \lambda^3 + 1 \\ 2\lambda^3 - \lambda^2 - \lambda + 3 & 2\lambda^3 - \lambda^2 - \lambda + 2 \end{pmatrix} \sim \begin{pmatrix} 1 & \lambda^3 + 1 \\ 1 & 2\lambda^3 - \lambda^2 - \lambda + 2 \end{pmatrix}$$

From this, we get  $2\lambda^3 - \lambda^2 - \lambda + 2 \neq \lambda^3 + 1$ .

Simplifying the inequality, we find elementary divisors:

$$2\lambda^3 - \lambda^2 - \lambda + 2 \neq \lambda^3 + 1$$

$$\lambda^3 - \lambda^2 - \lambda + 1 \neq 0$$

$$(\lambda^3 + 1) - \lambda(\lambda + 1) \neq 0$$

$$(\lambda + 1)(\lambda - 1)^2 \neq 0$$

Elementary divisors of the given matrix

$$(\lambda + 1)(\lambda - 1)^2.$$

*Masala.*  $A = \begin{pmatrix} 1 & 1 \\ -1 & 3 \end{pmatrix}$  matritsaning  $A^{50}$  darajasini toping.

*Matter.* Find the degree  $A^{50}$  of the matrix  $A = \begin{pmatrix} 1 & 1 \\ -1 & 3 \end{pmatrix}$

$$\text{Solving. } A^2 = \begin{pmatrix} 1 & 1 \\ -1 & 3 \end{pmatrix} \cdot \begin{pmatrix} 1 & 1 \\ -1 & 3 \end{pmatrix} = \begin{pmatrix} 0 & 4 \\ -4 & 8 \end{pmatrix} = 2^2 \cdot \begin{pmatrix} 0 & 1 \\ -1 & 2 \end{pmatrix}$$

$$A^3 = 2^2 \cdot \begin{pmatrix} 0 & 1 \\ -1 & 2 \end{pmatrix} \cdot \begin{pmatrix} 1 & 1 \\ -1 & 3 \end{pmatrix} = 2^2 \cdot \begin{pmatrix} -1 & 3 \\ -3 & 5 \end{pmatrix}$$

$$A^4 = 2^2 \begin{pmatrix} -1 & 3 \\ -3 & 5 \end{pmatrix} \cdot \begin{pmatrix} 1 & 1 \\ -1 & 3 \end{pmatrix} = 2^2 \cdot 2^2 \cdot \begin{pmatrix} -1 & 2 \\ -2 & 3 \end{pmatrix} = 2^4 \cdot \begin{pmatrix} -1 & 2 \\ -2 & 3 \end{pmatrix}$$

From these relations, we define the following recurrence relation:

$$A^{50} = 2^{50} \cdot \begin{pmatrix} -24 & 25 \\ -25 & 26 \end{pmatrix}.$$

## CONCLUSION

In addition to mathematics, the department of matrices is taught to students of economics, biotechnology, psychology, chemistry, physics, and applied mathematics in higher educational institutions. During the study of matrices, students gain not only their professional knowledge, but also their thinking and worldview. increases. In the process of solving non-standard problems, the skill of using existing knowledge in unfamiliar situations is formed and developed.

## REFERENCES

1. Proskuryakov. Chiziqli algebra va analitik geometriya. Lan. Sank-Peterburg. Moskva. Krasnodar. 2010.
2. Noriyeva A. O“ QUVCHILARNING KREATIVLIK QOBILIYATLARINI RIVOJLANTIRISHDA NOSTANDART MISOL VA MASALALARING AHAMIYATI //Журнал математики и информатики. – 2022. – Т. 2. – №. 1.
3. Meliyeva Mohira Zafar qizi, & Noriyeva Aziza. (2023). KO‘PHADLARNI HOSILA YORDAMIDA KO‘PAYTUVCHILARGA AJRATISH . *ОБРАЗОВАНИЕ НАУКА И ИННОВАЦИОННЫЕ ИДЕИ В МИРЕ*, 20(3), 117–120. Retrieved from <http://newjournal.org/index.php/01/article/view/5708>
4. Нориева А. Кости тенсизлігі және үнинг қызықарлы масалаларға тәдбиqlari //Современные инновационные исследования актуальные проблемы и развитие тенденций: решения и перспективы. – 2022. – Т. 1. – №. 1. – С. 361-364.

5. Рабимкул А., Иброҳимов Ж. Б. ў., Пўлатов, БС and Нориева, АЖ қ. 2023. АРГУМЕНТЛАРНИ ГУРУҲЛАРГА АЖРАТИБ БАҲОЛАШ УСУЛИДА КЎП ПАРАМЕТРЛИ НОЧИЗИҚЛИ РЕГРЕССИЯ ТЕНГЛАМАЛАРИНИ ҚУРИШ МАСАЛАЛАРИ //Educational Research in Universal Sciences. – 2023. – Т. 2. – №. 2. – С. 174-178.
6. Abdunazarov R. Issues of effective organization of practical classes and clubs in mathematics in technical universities. Mental Enlightenment Scientific-Methodological Journal. Current Issue: Volume 2022, Issue 3 (2022) Articles.
7. Абдуназаров Р. О. численной решение обратной спектральной задачи для оператора Дирака //Журнал “Вопросы вычислительной и прикладной математики. – №. 95. – С. 10-20.
8. Отакулов С., Мусаев А. О. Применение свойства квазидифференцируемости функций типа минимума и максимума к задаче негладкой оптимизации //Colloquium-journal. – Голопристанський міськрайонний центр знятості, 2020. – №. 12 (64). – С. 48-53.
9. Мусаева А. О. Зарубежная система финансирования образовательных учреждений //Наука и новые технологии. – 2011. – №. 10. – С. 75-81.
10. Мусаев А. О. Интеграция образовательных систем России и Дагестана XIX века //Известия Дагестанского государственного педагогического университета. Психолого-педагогические науки. – 2010. – №. 3. – С. 21-24.